

Roll NO. \_\_\_\_\_

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**6E3093****6E3093****B.Tech VI Semester (Main/Back) exam. May, 2012****Electronics & Comm. Engg.****6EC6.3 Optimization Techniques****Time : 3 Hours****Maximum Marks : 80****Min. Passing Marks : 24***Instructions to Candidates:*

*Attempt any **five questions**, selecting one question from each unit. All Question carry equal marks. Schematic diagrams must be shown wherever necessary. Any data you feel missing suitably be assumed and stated clearly.*

*Units of quantities used/ calculated must be stated clerly.*

Use of following supporting material is permitted during examination. (Mentioned in form No. 205)

1. \_\_\_\_\_ Nil \_\_\_\_\_

2. \_\_\_\_\_ Nil \_\_\_\_\_

## Unit - I

1. (a) What is optimization technique? Write down a short note on engineering applications of optimization. 8
- (b) ABC Ltd is assembling two products  $P_1$  and  $P_2$ . The cost of assembling one unit of products  $P_1$  and  $P_2$  is Rs. 200 and Rs. 400 respectively. The availability of work station for two products is limited to 60 hours and the two products spend 6 hours and 2 hours respectively on the work station. The products can be sold for Rs. 280 and Rs. 320 respectively. Total man-hours available are 400 and  $P_1$  requires 2 man-hours and  $P_2$  requires 4 man-hours. Formulate the problem as a LPP. 8

Or

1. Write down a short note on “classification of optimization problems” based on following : 4x4=16

- (a) Classification based on the nature of the design variables
- (b) Classification based on the nature of the equations involved
- (c) Classification based on the permissible values of the design variables rtuonline.com
- (d) Classification based on the number of objective functions.

## Unit-II

2. (a) solve the following LPP by Big-M method:

$$\text{Min } Z = x_1 + x_2$$

$$\text{s.t. } 2x_1 + x_2 \geq 4$$

$$x_1 + 7x_2 \geq 7$$

$$\text{and } x_1, x_2 \geq 0$$

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- (b) Use revised simplex method to solve the following LPP

$$\text{Max } Z = x_1 + x_2$$

$$\text{s.t. } 3x_1 + 2x_2 \leq 6$$

$$x_1 + 4x_2 \leq 4$$

$$\text{and } x_1, x_2 \geq 0$$

8

Or

2. (a) Find the dual of the following LPP

$$\text{Max. } Z = x_1 + 3x_2$$

$$\text{s.t. } 3x_1 + 2x_2 \leq 6$$

$$3x_1 + x_2 = 4$$

$$\text{and } x_1, x_2 \geq 0$$

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- (b) Find the optimal solution of the given LPP

$$\text{Max } Z = 3x_1 + 5x_2$$

$$\text{s.t. } 3x_1 + 2x_2 \leq 18$$

$$x_1 \leq 4$$

$$x_2 \leq 6$$

$$\text{and } x_1, x_2 \geq 0$$

Discuss the effect on the optimality of the solution when the objective function is changed to  $Z = 3x_1 + x_2$

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### Unit-III

3. (a) Solve the following assignment problem

	P	Q	R	S	T
A	85	75	65	125	75
B	90	78	66	132	78
C	75	66	57	114	69
D	80	72	60	120	72
E	76	64	56	112	68

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- (b) Solve the following by Vogel's approximation method (VAM) and test its optimality by MODI method:

	I	II	III	IV	Supply ↓
A	4	6	8	13	50
B	13	11	10	8	70
C	14	4	10	13	30
D	9	11	13	8	50
Demand →	25	35	105	20	185 / 200

8

Or

- (a) Find the assignment of salesman to districts that will result in maximum sales

Salesman ↓ \ Districts →	A	B	C	D	E
1	30	38	40	28	40
2	40	24	28	21	36
3	41	27	33	30	37
4	22	38	41	36	36
5	29	33	40	35	39

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- (b) Solve the following by North West Corner Rule (NWCR) and test its optimality by MODI method. The shipping costs are given

	A	B	C	Capacity↓
W	4	8	8	56
X	16	24	16	82
Y	8	16	24	77
Requirement →	72	102	41	215

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### Unit-IV

4. (a) Minimize  $f(x_1, x_2) = 2x_1^2 + x_2^2$  by Steepest Descent method. The starting point is ( ) and solve upto two iterations. rtuonline.com 8

(b) Min  $f(x) = x^2 + 2y^2$

s.t.  $2x + 5y - 10 \leq 0$

by using exterior penalty method and final solutions for  $r=1, 10$  and  $r \rightarrow \infty$ .

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Or

Minimize  $f(x) = x_1 - x_2 + 2x_1^2 + 2x_1x_2 + x_2^2$  starting from the point  $x_1 (0^0)$  along the directions  $S = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$  by quadratic interpolation method with an initial step length to  $\approx 0.1$

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## Unit-V

5. (a) Determine the value of  $u_1$ ,  $u_2$  and  $u_3$  so as to

$$\text{maximize } Z = u_1 \cdot u_2 \cdot u_3$$

$$\text{s.t. } u_1 + u_2 + u_3 = 10$$

$$\text{and } u_1, u_2, u_3 \geq 0$$

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- (b) Solve the following LPP by dynamic program approach

$$\text{Max. } Z = 8x_1 + 7x_2$$

$$\text{s.t. } 2x_1 + x_2 \leq 8$$

$$5x_1 + 2x_2 \leq 15$$

$$\text{and } x_1, x_2 \geq 0$$

8

Or

5. (a) Use dynamic programming approach to solve

$$\text{Minimize } Z = y_1^2 + y_2^2 + \dots + y_n^2$$

$$\text{s.t. } y_1 + y_2 + y_3 + \dots + y_n = C; (C \neq 0)$$

$$\text{and } y_j \geq 0; j=1, 2, \dots, n.$$

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(b) Write down short notes on following

- (i) Stage
- (ii) State
- (iii) Return function
- (iv) Bellman's principle of optimality

2x4=8

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